# Esame di Lingua Inglese (1.5 ore)

# Confused bank teller

A confused bank teller transposed the dollars and cents when he cashed a check for Ms Smith, giving her dollars instead of cents and cents instead of dollars. After buying a newspaper for 50 cents, Ms Smith noticed that she had left exactly three times as much as the original check. What was the amount of the check?

Let x be the number of dollars in the check, and y be the number of cents. Consider the numbers of dollars and cents Ms Smith holds at various times. The original check is for x dollars and y cents. The bank teller gave her y dollars and x cents. After buying the newspaper she has y dollars and x-50 cents. We are also told that after buying the newspaper she has three times the amount of the original check; that is, 3x dollars and 3y cents. Then, bearing in mind that x and y must both be less than 100 (for the teller's error to make sense), we equate dollars and cents.

As  $-50 \le (x-50) \le 49$  and  $0 \le y \le 99$ , there is a relatively small number of ways in which we can equate dollars and cents. Clearly, 3y-(x-50) must be divisible by 100. Further, by the above inequalities,  $-49 \le 3y-(x-50) \le 347$ , giving us four multiples of 100 to check. We compute easily that there is only one integer solution; so the check was for \$18.56.

#### **ESERCIZI**

#### 1. SELEZIONARE IL CORRETTO COMPLETAMENTO

- 1. One dollar is (less than) (fewer than) (least than) 200 cents.
- 2. There are (no more) (much more) (many more) noninteger solutions to the problem.
- 3. She had (many) (much) (long) times the amount of the original check.
- 4. When (did) (do) (has) she notice the error?

## 2. TRADURRE IN INGLESE LE FRASI SEGUENTI

- 1. Un giornale costa 50 centesimi.
- 2. Il cassiere commette un errore.
- 3. Se ci fossero più soluzioni intere, il problema non sarebbe risolubile.
- 4. Un altro approccio consiste nello scrivere l'equazione 100y+x-50=3(100x+y) e cercarne soluzioni intere con l'algoritmo euclideo.

### 3. TRADURRE IN ITALIANO IL TESTO