

$\lim_{x \rightarrow +\infty} x^\alpha = +\infty$	$\alpha > 0$	$\lim_{x \rightarrow +\infty} x^\alpha = 0$	$\alpha < 0$
$\lim_{x \rightarrow +\infty} a^x = +\infty$		$\lim_{x \rightarrow -\infty} x^a = 0$	$a > 1$
$\lim_{x \rightarrow +\infty} a^x = 0$		$\lim_{x \rightarrow -\infty} a^x = +\infty$	$a < 1$
$\lim_{x \rightarrow +\infty} \log_a(x) = +\infty$		$\lim_{x \rightarrow 0^+} \log_a(x) = -\infty$	$a > 1$
$\lim_{x \rightarrow +\infty} \log_a(x) = -\infty$		$\lim_{x \rightarrow 0^+} \log_a(x) = +\infty$	$a < 1$

**Tavola I** Limiti di funzioni elementari

$\lim_{x \rightarrow 0} \frac{\sin(x)}{x} = 1$		$\lim_{x \rightarrow 0} \frac{1 - \cos(x)}{x^2} = \frac{1}{2}$
$\lim_{x \rightarrow 0} \left(1 + \frac{a}{x}\right)^x = e^a$	$a \in \mathbf{R}$	
$\lim_{x \rightarrow 0} (1 + x)^{\frac{1}{x}} = e$	$a \in \mathbf{R}$	
$\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \log(a)$	$a > 0$	
$\lim_{x \rightarrow 0} \frac{\log_a(1 + x)}{x} = \log_a(e)$	$a > 0$	
$\lim_{x \rightarrow 0} \frac{(1 + x)^\alpha - 1}{x} = \alpha$	$\alpha \in \mathbf{R}$	

**Tavola II** Limiti notevoli.

**Tavola I. Formule di Mac Laurin con resto di Peano**

$$e^x = 1 + x + \frac{x^2}{2} + \dots \dots + \frac{x^n}{n!} + o(x^n)$$

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} \dots \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + o(x^{2n+2})$$

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} \dots \dots + (-1)^n \frac{x^{2n}}{(2n)!} + o(x^{2n+1})$$

$$\arcsin(x) = x - \frac{x^3}{3} + \frac{x^5}{5} \dots \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)} + o(x^{2n+2})$$

$$\operatorname{arctg}(x) = x - \frac{x^3}{3} + \frac{x^5}{5} \dots \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)} + o(x^{2n+2})$$

$$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} \dots \dots + (-1)^{n-1} \frac{x^n}{n} + o(x^n)$$

$$\operatorname{tg}(x) = x + \frac{x^3}{3} + \frac{2x^5}{5} + \frac{17x^7}{315} + o(x^8)$$

$$(1+x)^\alpha = 1 + \alpha x + \binom{\alpha}{2} x^2 \dots \dots + \binom{\alpha}{n} x^n + o(x^n)$$

In particolare

$$\frac{1}{1-x} = 1 + x + x^2 \dots \dots + x^n + o(x^n)$$

$$\frac{1}{1+x} = 1 - x + x^2 \dots \dots + (-1)^n x^n + o(x^n).$$

<b>Tavola I. Formule di Mac Laurin con resto di Lagrange</b>
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$$e^x = 1 + x + \frac{x^2}{2} + \dots \dots + \frac{x^n}{n!} + \frac{x^{n+1}}{(n+1)!} e^c$$

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} \dots \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + (-1)^{n+1} \frac{x^{2n+2}}{(2n+2)!} \sin(c)$$

$$\sin(x) = x - \frac{x^3}{3!} + \frac{x^5}{5!} \dots \dots + (-1)^n \frac{x^{2n+1}}{(2n+1)!} + (-1)^{n+1} \frac{x^{2n+3}}{(2n+3)!} \cos(c)$$

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} \dots \dots + (-1)^n \frac{x^{2n}}{(2n)!} + (-1)^{n+1} \frac{x^{2n+1}}{(2n+1)!} \sin(c)$$

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} \dots \dots + (-1)^n \frac{x^{2n}}{(2n)!} + (-1)^{n+1} \frac{x^{2n+2}}{(2n+2)!} \cos(c)$$

$$\log(1+x) = x - \frac{x^2}{2} + \frac{x^3}{3} \dots \dots + (-1)^{n-1} \frac{x^n}{n} + (-1)^n \frac{x^{n+1}}{n+1} \frac{1}{(1+c)^{n+1}}$$

$$(1+x)^\alpha = 1 + \alpha x + \binom{\alpha}{2} x^2 \dots \dots + \binom{\alpha}{n} x^n + \binom{\alpha}{n+1} (1+c)^{\alpha-n-1} x^{n+1}$$

dove  $\binom{\alpha}{k} = \frac{\alpha(\alpha-1)(\alpha-2)\dots(\alpha-k+1)}{k!} \quad \alpha \in \mathbf{R}$

$e^x$	$= 1 + x + \frac{x^2}{2} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} \frac{x^n}{n!}$
$\sin(x)$	$= x - \frac{x^3}{3!} + \frac{x^5}{5!} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)!} =$
$\cos(x)$	$= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n}}{(2n)!}$
$\arcsin(x)$	$= x - \frac{x^3}{3} + \frac{x^5}{5} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)}$
$\arctg(x)$	$= x - \frac{x^3}{3} + \frac{x^5}{5} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^n \frac{x^{2n+1}}{(2n+1)}$
$\log(1+x)$	$= x - \frac{x^2}{2} + \frac{x^3}{3} + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^{n-1} \frac{x^n}{n}$
$\operatorname{tg}(x)$	$= x + \frac{x^3}{3} + \frac{2x^5}{5} + \frac{17x^7}{315} + \dots\dots\dots$	
$(1+x)^\alpha$	$= 1 + \alpha x + \binom{\alpha}{2} x^2 + \dots\dots\dots$	$= \sum_{n=0}^{\infty} \binom{\alpha}{n} x^n$
$\frac{1}{1-x}$	$= 1 + x + x^2 + \dots\dots\dots$	$= \sum_{n=0}^{\infty} x^n$
$\frac{1}{1+x}$	$= 1 - x + x^2 + \dots\dots\dots$	$= \sum_{n=0}^{\infty} (-1)^n x^n.$
$\sqrt{1-x}$	$= 1 + \frac{1}{2}x - \frac{1}{8}x^2 + \frac{1}{16}x^3 + \dots\dots\dots$	

**Tavola III** Serie di Taylor di punto iniziale 0 di alcune funzioni elementari

$$\binom{\alpha}{k} = \frac{\alpha(\alpha-1)(\alpha-2)\dots(\alpha-k+1)}{k!}$$

$$k \in \mathbf{N}, \alpha \in \mathbf{R}.$$